

1 Article

2 Different language modalities, yet similar cognitive 3 processes in arithmetic fact retrieval.

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11 **Abstract:** Does experience with signed language impact the neurocognitive
12 processes recruited by adults solving arithmetic problems? We use event-related
13 potentials (ERPs) to identify the components that are modulated by operation type
14 and problem size in Deaf American Sign Language (ASL) native signers and in
15 hearing English-speaking participants. Participants were presented with single-digit
16 subtraction and multiplication problems in a delayed verification task. Problem size
17 was manipulated in small and large problems with an additional extra-large
18 subtraction condition to equate the overall magnitude of large multiplication
19 problems. Results show comparable behavioral results and similar ERP dissociations
20 across groups. First, an early operation type effect is observed around 200ms post
21 problem onset, suggesting that both groups have a similar attentional differentiation
22 for processing subtraction and multiplication problems. Second, for the posterior-
23 occipital component between 240ms and 300ms, subtraction problems show a similar
24 modulation with problem size in both groups suggesting that only subtraction
25 problems recruit quantity-related processes. Control analyses exclude possible
26 perceptual and cross-operation magnitude-related effects. These results are the first
27 evidence that the two operation types rely on distinct cognitive processes within the
28 ASL native signing population and that they are equivalent to those observed in the
29 English-speaking population.

25 **Citation:** Lastname, F.;
26 Lastname, F.; Lastname, F.
27 Title. *Brain Sci.* **2021**, *11*, x.
28 <https://doi.org/10.3390/xxxxx>

29 Academic Editor: Firstname
30 Lastname

31 Received: date
32 Accepted: date
Published: date

Keywords: Event-related Potentials; Arithmetic facts; Deaf native signers; Language
modality; Problem size effect; Operation type effect; American Sign Language.

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1. Introduction

Studies in arithmetical cognition have been focusing on how experience, training and teaching practices can impact the neurocognitive substrates supporting arithmetic processing [1]. So far, studies have shown real-time learning effects [2-5], focused strategies training effects [2, 5] and even cultural-linguistic differences [6] to determine the extent to which the neural substrates as well as the cognitive strategies used in arithmetic can be and are malleable. A question that has been overlooked is whether language modality, signed instead of spoken, may impact the neural network and strategies involved in single-digit arithmetic processing.

45 Sign languages, such as American Sign Language (ASL), are
46 complete natural languages that have the same linguistic
47 properties and complexity as spoken languages: they possess
48 grammatical rules, syntax, phonological and morphological
49 properties [7]. Signed languages are perceived visually and
50 expressed manually; thus, information is conveyed through
51 substantially different sensory modalities. Given that our brains
52 and cognitive processes are shaped by experience [8], it is not a
53 surprise that using a sign language, and not deafness, has been
54 shown to enhance or modify both cognitive and neural
55 processes [9-16]. Research has also shown that sign languages,
56 acquired early, rely on a network including the same left-
57 lateralized brain areas supporting spoken languages [13-18].
58 These studies have been central in demonstrating how the
59 neural substrates for language processing are function-
60 dependent and modality-independent [17]. However, much less
61 is known about the impact of language modality on the
62 neurocognitive processes supporting proficient arithmetic
63 processing. Here, we aim to investigate whether an early and
64 lifelong exposure to a visuo-manual language (i.e., a signed
65 language) combined with early profound to severe hearing loss
66 may modify the cognitive processes and neural response
67 involved in solving arithmetic problems.

68 So far, the literature in cognitive and neuro- science of
69 arithmetic has shown that different arithmetic operations are
70 mostly solved through different strategies that rely on partially
71 distinct brain networks [19-22]. Electrophysiological studies
72 support this distinction as well [23-25]. Subtraction problems
73 rely on procedures and quantity manipulation, whereas
74 multiplication problems rely on the phonological loop and
75 verbal retrieval of stored facts [26, 27]. Solving subtraction
76 problems relies on bilateral parietal and posterior areas
77 typically involved in quantity processing (intraparietal sulcus,
78 IPS) and visuospatial manipulation (posterior superior parietal
79 lobule, PSPL) [23, 26, 28]. Solving multiplication problems, on
80 the other hand, activates a left-lateralized network in the
81 temporal (superior and middle temporal gyri, STG and MTG)
82 and inferior frontal cortices (inferior frontal gyrus, IFG)
83 commonly activated in phonological processing [24, 26]. This
84 differentiation of brain networks appears to be experience-
85 driven, where practice and training increase the observed
86 neural differentiation [3-5, 28-30]. Additionally, problem size
87 has been shown to modulate the reliance on the different
88 networks, with larger problems being more likely solved
89 through computation-based strategies [26, 31-34]. An open
90 question is whether the differentiation between operation types
91 is related to language modality and if current findings are
92 therefore specific to the spoken language.

93 By comparing the electrophysiological correlates evoked by
94 multiplication and subtraction problems in hearing English
95 speaking and Deaf native ASL signing participants, we will be
96 able to test whether modality has an impact on the brain
97 functions involved and, if so, at which stage these come into

98 play. We chose the event-related potential approach as a first
99 investigation comparing the strategies used by Deaf native
100 signers and English-speaking participants. As Hinault and
101 Lemair [35] explain, the EEG method (i.e., either the ERP or
102 ERSP) can provide electrophysiological signatures in support of
103 different arithmetic strategies and show that these strategies
104 are implemented differently depending on problem size and
105 operation type. Here, we will leverage the strength of the EEG
106 method to investigate whether the Deaf native signers and
107 English-speaking participants show distinct electrophysiological
108 signatures and if these differ depending on the operation type
109 as well as problem size. We use a delayed verification paradigm
110 in which participants are presented with small and large single-
111 digit subtraction and multiplication problems as well as extra-
112 large subtraction problems. These two operation types have
113 shown the greatest dissociation in strategies and neural
114 correlates [21, 22]. We also added an extra-large subtraction
115 condition to equate the overall numerical magnitude of large
116 single-digit multiplication problems. In our English-speaking
117 control group, we expect to see differences related to operation
118 type in the earlier time windows (i.e., components). Prior
119 studies have suggested that the early modulations are
120 indicative of differential allocation of attentional resources
121 supporting distinct cognitive strategies [23-25, 36]. Only one
122 study identified differences as early as 100ms post problem
123 onset [37], whereas most other studies found differences
124 beyond 200ms and up to 300ms following problem onset [23-
125 25]. Because prior research has shown that Deaf native signers
126 recruit similar left-lateralized language areas for language
127 processing, and if these language-based processes are also
128 uniquely supporting multiplication-specific retrieval [26, 28],
129 we expect to find a similar early dissociation for the Deaf
130 signing group. Alternatively, research has also shown that
131 processing a sign language might recruit more bilateral fronto-
132 temporal brain areas as well as parietal areas supporting visuo-
133 spatial processes [13]. These additional processes related to
134 sign language could influence the neuro-cognitive processes
135 involved in solving arithmetic problems. Therefore, it is possible
136 that our Deaf native signing group either shows no distinction
137 between operations or shows a dissociation between the
138 operations at a different timepoint. If a lifelong exposure to a
139 signed language impacts how Deaf signers allocate resources
140 and attentional processes in relation to the two operation types,
141 we would expect an early interaction between group and
142 operation type were only our hearing participants show a
143 dissociation as observed in prior studies. In relation to
144 problems size, prior work has shown modulation over a late
145 component indicating greater use of computational instead of
146 retrieval strategies [30, 32, 33, 37]. This modulation is expected
147 to be stronger for subtraction problems as these have shown to
148 rely on computation [23, 26, 28]. Furthermore, the modulation
149 of the amplitudes on the later component will have to be
150 consistent with the three different levels of problem size for

151 subtraction problems. If our Deaf native signers were to rely on
152 retrieval for both problem types, we might not see a modulation
153 with problem size for subtraction problems at this later
154 component.

155 2. Materials and Methods

156 2.1. Participants

157 Participants were recruited through a mix of university and
158 local advertising strategies. An initial screening was performed
159 by email, and eligible participants were then invited to the lab.
160 To be included in the study, participants had to be between 18
161 and 35 years of age, either be native English speakers with no
162 hearing loss or native ASL signers (exposure before age 2)
163 identifying as Deaf and having used ASL during their formative
164 education (i.e., School for the Deaf, Deaf Program in
165 mainstream schools or interpreter support in mainstream
166 schools). After removing participants due to technical failures
167 (missing files, equipment failure, recording issues, $n = 9$) and
168 participants with low accuracy (below 70%: $n = 3$ English
169 speakers and $n = 2$ Deaf ASL Signers), 29 ASL native signers
170 and 35 English speakers were included in the analyses. The
171 mean age for the ASL native group was 23.7 years ($SD = 6.10$)
172 and for the English-speaking group was 27.2 ($SD = 8.06$). A t -
173 test revealed that age was not significantly different between
174 groups ($p > .1$). Gender distribution was 15 females and 14
175 males in the ASL native group and 24 females and 10 males,
176 with one participant declining to disclose the information for
177 the English-speaking group. A chi-square distribution showed
178 that gender across groups was not significantly different from
179 random ($\chi^2 = 2.36$, $p > .1$). All but one English-speaking
180 participant were right-handed.

181 2.2. Procedure

182 While participants were being fitted with the EEG cap, they
183 signed the consent form, responded to a demographic
184 questionnaire, and answered our language background survey.
185 To ensure optimal communication for all participants, the
186 testing team was composed of Deaf native signers as well as
187 fluent English speakers. All Deaf participants were provided
188 instruction in ASL, while all hearing participants were provided
189 instructions in spoken English. The duration of the entire
190 session was between an hour and an hour and a half, including
191 set up. The project was approved by the University's
192 Institutional Review Board.

193 The task consisted of a delayed operation verification task of
194 multiplication and subtraction problems. Problems could be
195 single-digit small and large multiplication problems or single-
196 digit small, large, and two-digit extra-large subtraction
197 problems (see list of problems in annex 1). Extra-large
198 problems were included to control for numerical magnitude and
199 were created using the solution to large multiplication
200 problems as minuend and one of the factors as the subtrahend.

201 The delayed design was used to lock the ERP to the problem
202 onset and model the ERP response for solving the operation
203 rather than assessing answer plausibility or storage access.

204 Each problem was presented four times with the incorrect
205 solution, twice per manipulation, and four times with the
206 correct solution. These were created based on prior literature
207 and depending on the operation [26, 37]. For multiplication
208 problems, the incorrect solution was the answer to an adjacent
209 problem in the same multiplication table. Each problem was
210 presented twice with the solution to the problem right before
211 and twice with the solution right after in the table. For
212 example, 3×5 was presented twice with answer 10 (2×5) and
213 twice with answer 20 (4×5). Additionally, the problem 5×3
214 was considered a distinct problem and presented with its own 2
215 incorrect solutions (12 and 18). For small and large subtraction
216 problems, incorrect answers were created by adding or
217 subtracting 1 or 2 from the correct solution, but for extra-large
218 problems, they were created by adding or subtracting 2.
219 Because subtraction problems rely on procedures, it was
220 necessary to control for the parity of the proposed solution.

221 In total, 480 problems (96 in each condition) were presented
222 randomly in blocks of 48 trials (10 blocks). A trial would start
223 with a red fixation box for 300ms, then an operation sign (- or x)
224 appeared for 400ms before the problem was presented (Fig. 1).
225 This was done to avoid interference due to switching between
226 operations [38, 39]. The problem remained on the screen for
227 2000ms and was replaced by a blank screen of variable
228 duration. The duration was 600ms for small problems, 1000ms
229 for large problems, and 1200ms for extra-large problems to
230 provide participants with enough time to retrieve or calculate
231 the solution. Next, a proposed solution was presented for
232 800ms, for which participants only had to decide if it was
233 accurate or not and hold their response to avoid motor
234 components. On the following screen, a green check and red
235 cross appeared until participants gave their response.
236 Participants pressed the key ipsilateral to the green check if
237 they thought the proposed solution was accurate or by pressing
238 the key ipsilateral to the red cross if they thought the answer
239 was wrong. The side of appearance for the green check and red
240 cross was counterbalanced and random to avoid motor
241 preparation related to the response production. The trial was
242 then followed by a blank screen with a random duration
243 between 700 and 1200ms (i.e., SOA).
244

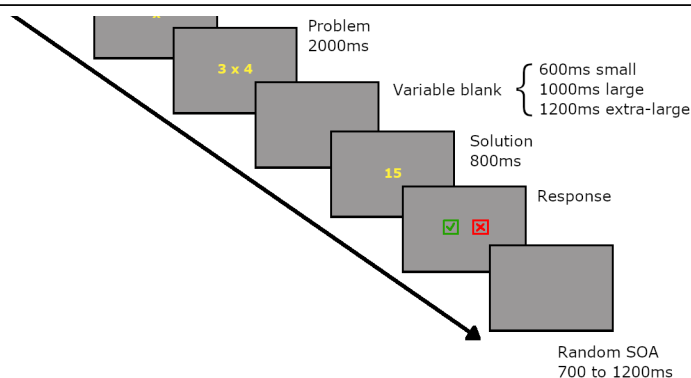


Figure 1. Schematic representation of a trial starting with a red fixation square for 300ms, followed by a yellow multiplication or subtraction sign for 400ms. The problem was then presented in yellow for 2000ms, followed by a variable blank of 600ms for small problems, 1000ms for large problems, and 1200ms for extra-large problems. The solution was presented for 800ms, and participants answered by selecting the green check or the red cross for correct or incorrect proposed solutions only on the next screen. The side of the presentation of the green check and red cross were counterbalanced and randomly presented. Participants would then press the f key or the j key on the keyboard ipsilateral to their selection. The response screen remained until participants gave their answer or for a maximum of 5000ms.

2.3. Electroencephalography data acquisition and preprocessing

The EEG was recorded using an actiCAP setup (Brain Products GmbH, Germany) with 64 active Ag/AgCl electrodes and SuperVisc gel. The 64 channels were placed based on the 10/20 system onto caps of different sizes to fit the participant's head optimally. EEG data was recorded at a rate of 1000Hz with Cz as reference and AFz as ground with a low pass filter set at 280Hz. Each electrode had an active amplifier and was connected to a 24-bit actiCHAMP amplifier for signal amplification (Brain Vision LLC, Morrisville, NC). The impedance of all electrodes was kept at or below 50k.

Preprocessing was performed using EEGLAB v2021.0 and the following toolboxes: PerpPipeline v0.55.4, Clean_rawdata v2.3, ICLabel v.1.3, and ERPLAB v8.10. Individual recordings were resampled to 250Hz. A high-pass 0.5Hz filter at -6dB with a transition bandwidth of 0.5Hz (i.e., passband edge 0.25-0.75 Hz) was applied. An initial data cleaning was computed with PrepPipeline (v0.55.4) to remove line noise. Clean-rawdata (v2.3) with conservative parameters was used to reject bad channels and correct continuous data using Artifact Subspace Reconstruction (ASR). This was done to allow for subsequent optimal independent component analysis (ICA). Removed channels were then interpolated before the average re-referencing. Finally, the ICA was performed to remove eye blinks. These were identified with ICLabel and thorough inspection of the activity power spectrum graph. On average, 2.41 (SD=.84) and 2.43 (SD=1.12) components were identified as eye blinks and removed for the ASL native signers and English-speaking groups, respectively.

286 To identify ERP components and the processes related to
287 solving the arithmetic problem, epochs were created based on
288 problem onset. The epochs start -500ms before the problem
289 onset ($t=0$) and continue until 2500ms after. Residual artifacts
290 were identified, and epochs with a peak-to-peak difference
291 beyond 150 μ v were removed, using a 200ms moving window
292 and a 100ms step over the duration of the entire epoch. For
293 each participant, trials were averaged for each condition only
294 for correct trials to avoid error-related noise. On average, 365
295 (SD=96) epochs over a total of 480 were retained for the ASL
296 native signers and 371 (SD=74) epochs for the English-
297 speaking group ($p>.1$). The entire duration before stimulus
298 onset (-500ms) was used as the baseline.

299 *2.4. ERP Components and analyses*

300 To independently identify ERP components, time windows,
301 and regions of interest (ROIs) for further analyses, we created
302 the grand average waveforms across all conditions and across
303 both groups. Observing the waveforms across the scalp and
304 the topographical maps, we identified the following seven
305 components (Fig. 2): a first centro-posterior negativity between
306 70ms and 110ms over [PO3, POz, PO4, Oz]; a second negativity
307 between 110ms and 140ms over the fronto-central electrodes
308 [C1, Cz, C2, FC1, FCz, FC2]; a first fronto-central positivity
309 between 180ms and 210ms over [FC1, F3, F1, AF3], [FC2, F4,
310 F2, AF4] and [FCz, Fz, AFz]; at a similar timing, a bilateral
311 parieto-occipital negativity between 180ms and 220ms over
312 [PO8, PO4, P8, P6] and [PO7, PO5, P7, P5]; a successive more
313 central negativity encompassing the entire occipital and
314 parietal channels between 240ms and 300ms over [O1, Oz, O2,
315 PO7, PO3, POz, PO4, PO8, P7, P5, P6, P8]; a centro-posterior
316 positivity between 310ms and 350ms over [CP1, CPz, CP2, P1,
317 Pz, P2]; and finally, a long and late positive-going component
318 around 400ms until 800ms over the centro-posterior channels
319 [P1, Pz, P2, CP1, CPz, CP2, C1, Cz, C2]. Time windows were
320 created to ensure that the peaks for each channel comprising
321 the ROI were within the time window while also avoiding the
322 peaks of successive components.
323

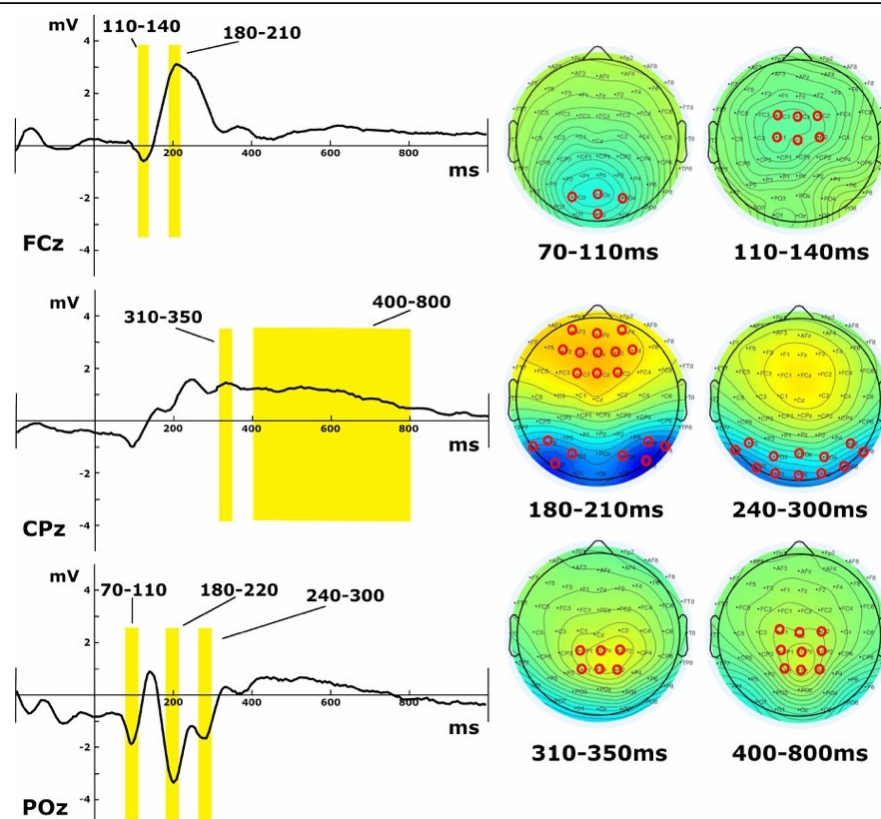


Figure 2. ERP and topographical representation of the seven components identified independently over the grand average waveforms computed across all tasks and across both groups. On the left, the components are identified by yellow windows over representative channels: FCz, CPz and POz. On the right, the topographical maps represent average variations of the grand average across the scalp, with the ROIs identified by red rings.

Average amplitudes for each condition and each participant were then extracted and analyzed with repeated measures ANOVAs. Operation type (subtraction vs. multiplication), and problem size (small vs. large) were entered as within-subject variables and group (ASL signers vs. English speakers) was entered as a between-subjects variable. For components showing bilateral peaks or asymmetric topographies, laterality (left, center and right, or left and right) was also entered as a within-subject factor. To further test whether specific components are related to problem size, a second set of repeated measures ANOVAs was performed entering the three subtraction sizes (i.e., small, large, and extra-large) as within-subjects and group as between-subjects. Finally, in instances where results needed further investigation to disentangle between competing explanations, further analyses have been performed and specified where appropriate. For all ANOVAs, the significance threshold was set at $\alpha = .05$. When the assumption of sphericity was not met, the Huynh-Feldt correction was applied, and the adjusted degrees of freedom are reported. We used the Benjamini-Hochberg False Discovery Rate [40] method to correct for multiple comparisons considering all planned ANOVAs over all components. To further investigate the interactions, the levels of the variables were tested with paired t-tests and the α was corrected using the Bonferroni method.

3. Results

3.1. Behavioral Results

Due to the experimental design, only task accuracy was analyzed. We first ran a repeated measures ANOVA with operation type and problem size as within-subject variables and group as between-subjects variables. The main effects of operation type ($F(1, 62) = 17.61, p < .001, \eta^2_p = .22$) and problem size ($F(1, 62) = 42.78, p < .001, \eta^2_p = .41$) were found to be significant. Responses to multiplication problems were more accurate than subtraction problems ($\mu = 94.5\%$ and $SD = 5.5\%$ for multiplication vs. $\mu = 90.3\%$ and $SD = 6.7\%$ for subtraction) and responses to small problems were more accurate than large problems ($\mu = 94.1\%$ and $SD = 3.3\%$ for small vs. $\mu = 88.6\%$ and $SD = 9.3\%$ for large). The interactions operation type by problem size ($F(1, 62) = 29.97, p < .001, \eta^2_p = .33$) and problem size by group ($F(1, 62) = 11.53, p = .001, \eta^2_p = .16$) were also found to be significant (Fig. 3). Post-hoc analyses, breaking down the operation type by problem size interaction, indicated that responses to small multiplication problems were significantly more accurate than large multiplication problems ($F(1, 63) = 74.90, p < .001, \eta^2_p = .54$; 96.6% vs. 88.4%) and more accurate than small subtraction problems ($F(1, 63) = 112.87, p < .001, \eta^2_p = .64$; 96.6% vs. 91.7%). The difference between small subtraction problems and large subtraction problems failed to reach significance (corrected $\alpha = .0125, p = .021$; 91.7% vs. 88.9%) as well as for large subtraction and large multiplication problems ($p = .56$; 88.9% vs. 88.4%). Breaking down the problem size by group interaction, no group differences survived the multiple comparison (for small problems $p > .05$ and for large problems $p = .045$). Problem size, analyzed separately for each group, was significant only for ASL signers with responses to small problems being more accurate than large ones ($F(1, 28) = 36.28, p < .001, \eta^2_p = .56$; 94.9% vs. 86.1% for ASL signers; $p = .013$; 93.5% vs. 90.7% for English speakers).

We further tested with a repeated-measures ANOVA the three levels of the subtraction problems. Problem size was entered as a within-subject variable and group as a between-subjects. Only problem size survived multiple comparison correction showing a linear decrease in accuracy with increasing problem size ($F(1.9, 117.8) = 15.48, p < .001, \eta^2_p = .20$; 91.7%, 88.9%, and 86.3% from smallest to largest condition). Accuracies from small to extra-large for ASL signers were: 92.6%, 87.0%, and 83.7%; and for the English-speaking participants accuracies were: 90.9%, 90.5%, and 88.5%.

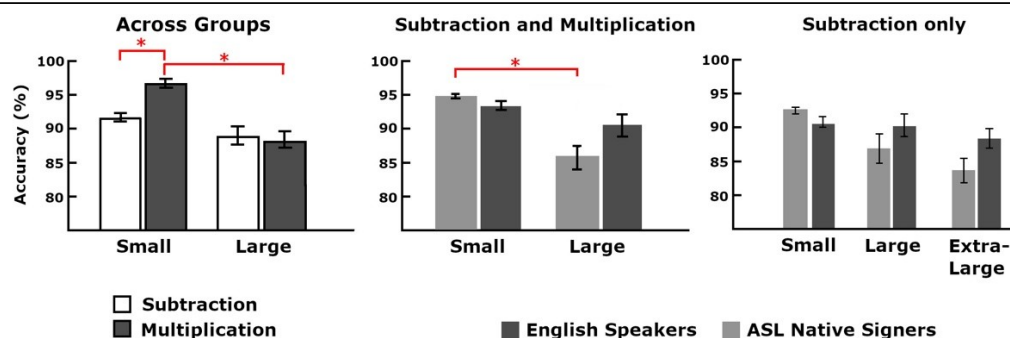


Figure 3. Graphs show percent accuracies for the three significant interactions: operation type by problem size across the two groups on the left, group by problem size across both operation types in the center, and problem size by group for the three levels of subtraction. Despite significant interactions, between-group differences do not reach significance.

3.2. ERP problem-locked components results

3.2.1. Centro-posterior negativity between 70ms and 110ms.

The repeated measures ANOVA with operation type and problem size as within-subject factors and group as between-subjects variable revealed a significant effect of operation type ($F(1, 62) = 16.56, p < .001, \eta^2_p = .21$) and problem size ($F(1, 62) = 14.99, p < .001, \eta^2_p = .19$) but not group, nor any interaction. Subtraction problems and large problems yielded greater negativity at this stage (subtraction problems: $-1.42 \mu\text{V}$, multiplication problems: $-1.05 \mu\text{V}$, large problems $-1.37 \mu\text{V}$, and small problems: $-1.1 \mu\text{V}$).

A second repeated measures ANOVA with problem size (small, large, and extra-large) as within-subjects and group as between-subjects variables was also run for subtraction problems. Only the main effect of problem size was found significant ($F(2, 124) = 5.51, p = .005, \eta^2_p = .08$; $-1.25 \mu\text{V}$, $-1.58 \mu\text{V}$ and $-1.34 \mu\text{V}$ for small, large and extra-large, respectively). Large subtraction problems were significantly more negative compared to both small and extra-large problems (corrected $\alpha = .017$ for paired t-tests: $t(63) = 3.07, p = .003$ for small vs. large; $t(63) = -2.46, p = .017$ for large vs. extra-large). No difference was found between small and extra-large problems ($p > .1$)

3.2.2. Fronto-central negativity between 110ms and 140ms.

For the operation type by problem size by group analysis, we only found a main effect of group where ASL signers showed greater negativity compared to English-speaking participants ($F(1, 62) = 9.83, p = .003, \eta^2_p = .14$; $-.77 \mu\text{V}$ vs. $-.05 \mu\text{V}$ for ASL signers and English speakers, respectively).

The repeated measure ANOVA comparing the three subtraction problem sizes again revealed a group effect ($F(1, 62) = 9.64, p = .003, \eta^2_p = .14$; $-.80 \mu\text{V}$ vs. $-.01 \mu\text{V}$ for ASL signers and English speakers, respectively).

3.2.3. Fronto-central positivity between 180ms and 210ms.

442 For this component, the peak appeared skewed to the left,
443 therefore, laterality (left, center, and right) was added to the
444 other 3 variables (operation type, problem size and group).
445 Group was the only between-subjects variable. Laterality
446 showed a significant result ($F(1.49, 92.95) = 7.9, p = .002, \eta^2_p = .11$;
447 $2.55 \mu\text{V}$ left, $2.63 \mu\text{V}$ center, and $2.31 \mu\text{V}$ right) with
448 post-hoc paired t-test showing that the right channels were less
449 positive compared to the central ones (corrected $\alpha = .017$ for
450 paired t-tests: $t(63) = 4.72, p < .001$ for center vs. right; $t(63) =$
451 $2.28, p = .026$ for left vs. right; $p > .1$ for left vs. center).
452 Operation type was also significant with greater positivity for
453 subtraction problems ($F(1, 62) = 9.2, p = .004, \eta^2_p = .13$; 2.61
454 μV for subtraction and $2.38 \mu\text{V}$ for multiplication). No other
455 effect was found.

456 The repeated measure ANOVA for the three subtraction
457 sizes, laterality and group, only returned a significant effect of
458 laterality ($F(1.66, 103.11) = 7.81, p = .001, \eta^2_p = .11, 2.6 \mu\text{V}$ for
459 left, $2.72 \mu\text{V}$ for center, and $2.38 \mu\text{V}$ for right). Post-hoc tests
460 showed a significant difference for the right channels being less
461 positive than the center ones (corrected $\alpha = .017$ for paired t-
462 tests: $t(63) = 4.66, p < .001$ for center vs. right; $t(63) = 2.05, p$
463 $= .044$ for left vs. right; $p > .1$ for left vs. center).
464

465 3.2.4. Bilateral parieto-occipital negativity between 180ms and 466 220ms.

467 This component appeared to show bilateral peaks,
468 therefore, laterality with left and right was entered with the
469 other variables into the repeated measures ANOVA. Right
470 channels were more negative than left channels ($F(1, 62) =$
471 $7.09, p = .01, \eta^2_p = .10$; $-4.03 \mu\text{V}$ and $-4.68 \mu\text{V}$). No other effects
472 were significant.

473 The repeated measures ANOVA for the three subtraction
474 problem sizes also included laterality (left and right) in addition
475 to group. Again, laterality was significant ($F(1, 62) = 7.93, p$
476 $= .006, \eta^2_p = .11$; $-4.03 \mu\text{V}$ and $-4.68 \mu\text{V}$ for right and left
477 channels, respectively) as well as problem size ($F(2, 124) =$
478 $5.12, p = .007, \eta^2_p = .08$) with small problems averaging -4.47
479 μV , large problems $-4.48 \mu\text{V}$, and extra-large problems -4.22
480 μV . Post-hoc paired t-test revealed that extra-large problems
481 were less negative than the two other problem sizes (corrected
482 $\alpha = .0167$ for paired t-tests: $t(63) = 2.49, p = .015$ for small vs.
483 extra-large; $t(63) = 3.21, p = .002$ for large vs. extra-large; p
484 $> .1$ for small vs. large problems).
485

486 3.2.5. Second parieto-occipital negativity between 240 and 487 300ms.

488 The repeated measures ANOVA included only operation
489 type, problem size, and group. The main effects of operation
490 ($F(1, 62) = 23.6, p < .001, \eta^2_p = .28$) and size ($F(1, 62) = 13.54,$
491 $p < .001, \eta^2_p = .18$) were significant with multiplication
492 problems being more negative than subtraction problems (-2.8

493 μV and $-2.34 \mu\text{V}$) and with small problems being more negative
494 than larger ones ($-2.67 \mu\text{V}$ and $-2.46 \mu\text{V}$). The main effect of
495 group was not significant.

496 The operation type by problem size interaction was also
497 significant ($F(1, 62) = 13.12, p = .001, \eta^2_p = .18$). Subtraction
498 problems showed modulation for problem size with smaller
499 problems being more negative than large problems ($F(1, 63) =$
500 $20.21, p < .001, \eta^2_p = .24; -2.53 \mu\text{V}$ and $-2.15 \mu\text{V}$).
501 Multiplication problems did not show a significant modulation
502 for size ($p > .1$). Both small and large problems were
503 significantly more negative for multiplication than subtraction
504 problems ($F(1, 63) = 8.63, p = .005, \eta^2_p = .12; -2.53 \mu\text{V}$ and $-$
505 $2.82 \mu\text{V}$ for small subtraction and small multiplication,
506 respectively; and $F(1, 63) = 27.83, p < .001, \eta^2_p = .30; -2.15 \mu\text{V}$
507 and $-2.78 \mu\text{V}$ for large subtraction and large multiplication,
508 respectively). Importantly, there were no interactions with
509 group (Fig. 4).

510 Analyzing problem size for subtraction problems, we only
511 found a main effect of size with a linear increase in amplitudes
512 with increasing numerical size ($F(2, 124) = 22.09, p < .001, \eta^2_p$
513 $= .26$, with a significant linear trend $F(1, 62) = 35.28, p < .001$;
514 average amplitudes of $-2.53 \mu\text{V}$ for small, $-2.15 \mu\text{V}$ for large and
515 $-1.96 \mu\text{V}$ for extra-large; post-hoc paired t-test comparisons
516 with corrected $\alpha = .025$: small vs. large $p < .001$, large vs.
517 extra-large only close to significance with $p = .03$). No other
518 effects were found.

519 To test that the modulation of this component was not
520 related to the numerical magnitude of the problems itself but
521 depended on the cognitive process involved based on the
522 operation, we directly compared large multiplication problems
523 with extra-large subtraction problems as these were equated on
524 overall magnitude. The repeated measure ANOVA with
525 operation type as within-subject and group as between-subjects
526 returned a significant operation type effect ($F(1, 62) = 43.66, p$
527 $< .001, \eta^2_p = .41$) with extra-large subtraction problems being
528 significantly less negative than multiplication problem ($-1.96 \mu\text{V}$
529 and $-2.78 \mu\text{V}$ for extra-large subtraction and large
530 multiplication problems, respectively). The effect of group was
531 again not significant.

532 Because extra-large problems were composed of two-digits
533 minus one-digit operations while large multiplication problems
534 were all single-digit operations, we also tested the possibility
535 that the difference was related to perceptual difference or
536 magnitude of the operands/minuends/subtrahends. Therefore,
537 we ran a repeated-measures ANOVA with small subtraction
538 problems and small multiplication problems only. These are
539 highly similar in numerical magnitude and are all single-digit
540 operations, thus making them perceptually similar. The effect
541 was significant ($F(1, 63) = 8.63, p = .005, \eta^2_p = .12$) with small
542 multiplication being significantly more negative than small
543 subtraction problems: $-2.82 \mu\text{V}$ and $-2.53 \mu\text{V}$, respectively.
544

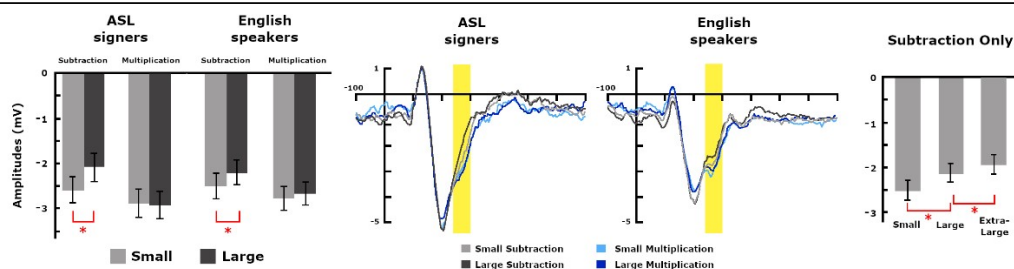


Figure 4. Modulation of amplitudes over the second posterior-occipital negativity between 240ms and 300ms. On the left, bars represent average amplitudes with standard errors for the two-way interaction, problem size by operation type, presented separately for each group for visualization purposes. In the center, the ERPs show average modulations over the parietal-occipital ROI for the time window between 240ms and 300ms (yellow highlight) for each group separately. On the right, the bars represent average modulations and standard errors for the three levels of the subtraction problems. Only subtraction problems show modulation with problem size over this component.

3.2.6. P300 Centro-posterior positivity between 310-350.

The repeated measures ANOVA with operation type, problem size and group showed only a main effect of group with ASL signers showing greater positivity ($F(1, 62) = 8.48, p = .005, \eta^2_p = .12$; $1.59 \mu\text{V}$ and $.91 \mu\text{V}$ for ASL signers and English speakers, respectively).

Investigating the three subtraction problem sizes, the repeated measures ANOVA again only returned a significant group effect with ASL signers showing more positive amplitudes ($F(1, 62) = 7.37, p = .009, \eta^2_p = .11$; $1.61 \mu\text{V}$ and $.98 \mu\text{V}$ for ASL signers and English speakers, respectively).

3.2.7. LPC Late centro-posterior positivity between 400ms and 800ms.

Finally, the analysis over the late, positive-going component only returned the main effects of problem size ($F(1, 62) = 7.38, p = .009, \eta^2_p = .11$). Small problems overall had more positive amplitudes ($.83 \mu\text{V}$ and $.73 \mu\text{V}$ for small and large problems).

The repeated measures ANOVA on the three levels of the subtraction problems returned a significant group effect with greater positivity for ASL signers ($F(1, 62) = 7.24, p = .009, \eta^2_p = .11$; $1.01 \mu\text{V}$ and $.60 \mu\text{V}$).

4. Discussion

In this experiment, we investigated whether a lifelong experience using a signed language would alter the neurocognitive processes involved in solving single digit arithmetic problems. To do so, we compared Deaf native ASL signers and English-speaking participants using the ERP approach. Based on prior literature, we tested the two operations known for being most distinct within the hearing and speaking population: subtraction and multiplication problems [21, 22]. These have shown to be solved through different procedures [41], rely on distinct brain networks [26, 28] and modulate ERP components differently [23, 25]. So far, one study investigated language modality and arithmetic processing using the fMRI [42]. Our study is unique as it is the first to investigate the impact of language modality on the time

590 course of arithmetic processing. It is only assumed that the
591 current models are independent of language modality and that
592 native sign language users rely on the same cognitive processes
593 as observed with hearing-speaking participants.

594 Behaviorally, the two groups performed overall equally well,
595 and the main effects of problem size and operation type were
596 found. Performance was overall highest for small multiplication
597 problems, but no significant difference was observed for large
598 problems across operation types. Deaf native signers showed a
599 stronger problem size effect across both operations. Moreover,
600 both groups showed a linear decrease in performance with
601 increasing size for subtraction problems. Overall, both groups
602 show similar behavioral effects for problem size and operation
603 type.

604 For the analysis of the neural signatures, we calculated the
605 ERPs in response to the presentation of the problem and
606 independently identified seven components. The first four
607 components appear within the 200ms post problem onset and
608 are likely related to early visual and attentional processes [43]
609 but that is also the time-window where different ERP studies
610 have shown that strategy selection can already occur (large 2-
611 digit problems [44]; split effects [45-48]). The remaining three
612 may be considered later components and more susceptible to
613 numerical quantity processing [32, 33, 37, 49].

614 The first centro-posterior negativity between 70 and 110ms,
615 shows modulation that is consistent with the visuo-spatial
616 properties of the stimuli. Indeed, amplitudes are more negative
617 overall for subtraction problems compared to multiplication
618 problems and this could be due to large subtraction problems
619 being composed of two digits minus one digit. A pattern
620 suggesting activations related to the visual properties also
621 appears in the analysis on the three levels of the subtraction
622 problems. Although the patterns are not completely consistent
623 with the variations in number of digits in the subtraction
624 problems, patterns are also not related to any magnitude
625 variation within the problems. Importantly, they do not show
626 any interaction suggesting early different processes occurring
627 between the two groups. Given the very early component, the
628 patterns are more likely explained by visuo-perceptual
629 variations in the stimuli.

630 For the second fronto-central negativity between 110 and
631 140ms, we only find a group effect where ASL signers show
632 greater negativity compared to English-speaking participants.
633 Although we did not predict this result, studies on visual
634 processing with congenitally deaf participants [50, 51] have
635 shown modulation of the visual-evoked potentials with greater
636 negativity in the deaf group compared to the hearing group
637 within this time window. This early modulation is interpreted as
638 plasticity changes increasing the reliance on visual input. Our
639 Deaf participants reported early, severe to profound hearing
640 loss, which is consistent with prior results suggesting that a
641 lack of early auditory input might have provided greater visuo-
642 attentional resources.

643 Next, we found a fronto-central positivity between 180 and
644 210ms showing a lateralized modulation by operation. The left
645 and central ROI channels were more positive than the right
646 channels, and subtraction problems were more positive
647 compared to multiplication problems. The absence of a size
648 effect suggests that this component is not sensitive to the
649 numerical magnitude but rather is related to the attentional
650 and cognitive processes differently involved in the two
651 operations. Regarding the operation type effect, it is known
652 from prior literature that multiplication problems engage more
653 left-lateralized processes compared to subtraction problems
654 [23, 26]. Zhou and colleagues [23], using ERPs, found
655 lateralized effects for multiplication problems showing greater
656 negativity over the frontal electrodes at around 320ms. These
657 effects were localized, through dipole source localization, in the
658 left anterior brain and interpreted as greater reliance on
659 phonological processes for multiplication problems compared to
660 subtraction and addition problems. Consistent with these
661 findings, we also find lower amplitudes for multiplication
662 compared to subtraction problems; however, the effect appears
663 over 100ms earlier in our study. This timing difference could
664 potentially be explained by differences in paradigm design. We
665 intentionally presented the operation sign before the full
666 problem to avoid trial-to-trial interference and cross-operation
667 errors [38, 52, 53]. But most importantly, behavioral work has
668 shown that presenting the operation sign before the full
669 problems decreases the response time for subtraction and
670 addition problems selectively [41]. Although our paradigm does
671 not allow to test for differences in response times, it is possible
672 that priming the operation sign induced faster cognitive
673 processing. Participants could have been ready to allocate
674 resources differently by operation at an earlier time than in the
675 study of Zhou and colleagues [23], where the full problem was
676 presented at once. Interestingly, another study by Muluh and
677 colleagues [36] presenting the full problem at once, also
678 reported early operation differences on the P100 and P200
679 components post problem onset, thus as early as 100ms to
680 150ms. They interpret these early operation-related
681 modulations as possible attention allocation differences, such as
682 the orientation of brain resources, for encoding the operation
683 signs and identifying the operation to be performed. Other
684 studies using different paradigms than ours and specifically
685 investigating strategy selection have found evidence for
686 modulations related to differences in strategies already
687 occurring in the first 200ms window [44-48]. Therefore, given
688 our paradigm, prior results and predictions, it is likely that our
689 observed operation-related modulation around 200ms is
690 indicative of an early strategy selection that might favor
691 phonological processing for multiplication problems. Most
692 importantly to the present research question is that there was
693 no modulation related to group at this early stage. This is the
694 first evidence that the early differential processes involved for

695 the two operations are likely to be similar regardless of the
696 language modality used.

697 At a similar timing, but in the bilateral posterior areas, a
698 negative component was observed between 180ms and 220ms.
699 Interestingly, the topographical maps in Muluh and colleagues
700 [36] show a similar bilateral negativity between 200ms and
701 250ms and to be stronger for subtractions than multiplications
702 but the paper does not report any statistical data on this
703 component. Our results showed that the right channels,
704 subtraction problems, and ASL signers were overall more
705 negative. Furthermore, investigating problem size within
706 subtraction problems, we find again greater right-lateralized
707 negativity as well as a problem size effect. The modulation with
708 problem size is interesting as it does not appear to reflect a
709 consistent modulation with either the visual properties of the
710 problems or the numerical size. Extra-large problems were less
711 negative than both small and large problems. A modulation
712 based on size would predict a more gradual change in
713 amplitudes for the three sizes. If this modulation were related
714 to visual properties, both large and extra-large problems would
715 show similar modulation given that both types of problems are
716 2-digits minus 1-digit operations. However, small and large
717 subtraction problems, which differ on the number of digits,
718 were not significantly different. This component could be, in
719 part, showing complementary modulations to those observed
720 simultaneously in the frontal positivity, that is operation and
721 lateralization effects, as well as emerging components more
722 clearly visible in the successive time window. Indeed, group and
723 size effects appear to emerge and continue to modulate
724 activations in the second posterior negativity.

725 In the second posterior negativity (Fig. 4), between 240ms
726 and 300ms, both operation type and problem size modulate the
727 electrophysiological response. In support of the argument that
728 the two consecutive posterior time windows indeed represent
729 different components, we found that multiplication problems
730 elicited greater negativity as opposed to subtraction problems
731 being more negative in the prior time window. Small problems
732 however continued to remain more negative than larger ones.
733 Additionally, modulations with problem size differed based on
734 operation type: the interaction was driven by a significant size
735 modulation within subtraction problems only. For both groups,
736 problem size was not significant for multiplication problems.
737 This result supports prior findings that the two operations are
738 solved through different processes [26]: Multiplication
739 problems failed to show a modulation with problem size and, as
740 shown in prior studies, this is consistent with the rote
741 memorization hypothesis; The modulation with problems size
742 for subtraction problems confirms the use of procedural and
743 quantity strategies. The analysis including the three problem
744 sizes for subtraction problems further confirms that the
745 component is modulated by the numerical size of the problem
746 as amplitudes showed a similar linear increase with increasing
747 problem size across groups (Fig. 4). Hence, this component is

748 most likely induced by processes that relate to quantity
749 manipulation.

750 Further analyses excluded that the modulation was related
751 to overall numerical magnitude given that large multiplication
752 problems were significantly more negative than extra-large
753 subtraction problems (equated on numerical magnitude) and
754 going in the opposite direction of the problem size modulation
755 observed for subtraction problems. Importantly, behavioral
756 analyses do not show any significant differences in performance
757 between these two conditions excluding differences in the
758 amount of attention or levels of performance. The ERP
759 difference again supports the idea that distinct cognitive
760 processes are occurring for the two operation types. Indeed,
761 the extra-large subtraction problems used here are unlikely to
762 be retrieved from long-term memory and thus required quantity
763 manipulation. Further, we also excluded that the difference
764 observed was related to the number of digits presented by
765 comparing single-digit small problems across operation types.
766 Despite being equated for number of digits and numerical
767 magnitude of the digits presented, amplitudes were
768 significantly different. Again, this confirms the difference in
769 strategies used for the two problems. Finally, and again most
770 relevant to the current study, we did not observe any
771 differences in amplitudes between groups for this component. It
772 appears that the differential recruitment of strategies for the
773 two types of problems holds similarly across the two groups.

774 Over the next component, the centro-posterior positivity
775 between 310 and 350, there was only a main difference of
776 group in both across and within operation analyses. ASL
777 signers showed an overall greater positivity. The P300 is
778 usually thought as an indication of attentional demands,
779 cognitive ability but also to be modulated by memory load.
780 Studies on memory have shown that decreases in amplitudes
781 were seen with increases in memory load [54]. Although the
782 two groups do not show differences in how their brain
783 responses differently modulate with operation type in the
784 preceding stage, it is still possible that they rely differently on
785 attentional and memory processes at later stages. Retrieving
786 and manipulating linguistic information in sign language might
787 recruit additional or different networks impacting this later
788 component [55]. Indeed, studies on the neural correlates of sign
789 language processes have shown both similar left-lateralized
790 language networks but also additional right and parietal
791 activations [18, 55].

792 Finally, the late component covering the large window from
793 400ms to 800ms showed a size effect and a group effect. This
794 late component has been reported previously to be present
795 specifically for problems requiring greater procedural
796 strategies. Núñez-Peña and colleagues [30, 32] named this
797 component the arithmetic-related positivity. In their results,
798 this component was stronger for subtraction problems
799 compared to addition problems [32] and for larger problems
800 compared to smaller ones [30]. In our data, we do not find any

801 operation differences, but we do find modulations driven by
802 problem size when both operation types are merged. The
803 direction of the modulation does not appear to be in line with
804 prior findings. In our data, small problems, those more likely to
805 be retrieved and less likely to be solved through procedural
806 strategies, had more positive amplitudes. Comparing the three
807 problem sizes for subtraction problems, we find a group
808 difference with ASL-signers showing greater amplitudes but no
809 problem size effect. The absence of the size effect suggests that
810 this component in our study might not be related to quantity
811 processing given our inclusion of extra-large problems certainly
812 requiring quantity manipulation. Looking into studies on
813 memory, specifically episodic memory, results have shown a
814 positivity over parietal channels where greater amplitudes were
815 related to greater retrieval success [56]. This could be more in
816 line with our findings since smaller problems generally tend to
817 rely more on memory retrieval. It is also possible that the two
818 groups differ in terms of episodic memory reliance. Because the
819 task resulted in several repetitions of the same problem, it is
820 plausible that participants recollected answers from a prior
821 calculation or prior retrieval. This could have been easier for
822 problems that were more easily answered, such as smaller
823 problems and, more speculatively, might be influenced by
824 language modality. It may be that using sign language,
825 compared to a spoken language, increases episodic memory
826 encoding while doing the task. This remains an interesting open
827 question.

828 Our results so far show that the two groups rely on similar
829 distinct attentional and quantity processing mechanisms for
830 solving subtraction and multiplication operations. These results
831 further support the idea that the cognitive processes recruited
832 while solving different arithmetic problems are independent of
833 the language modality used and, most likely, from the language
834 modality in which operations were learned. Based on the
835 recycling hypothesis, humans are not born with predefined
836 brain areas supporting higher-level arithmetical thinking [57].
837 It is through the recycling of older core systems that the human
838 mind can reach symbolic thought and mathematical reasoning.
839 What we observe here is that even through very different
840 prolonged language and sensory experiences, the distinction
841 between the operations remains, and the attentional and
842 cognitive processes involved are surprisingly similar across
843 groups. Subtle educational and short training manipulations
844 have shown changes in brain networks and strategies [3, 4];
845 how is it that the use of a visual and manual language does not
846 modify more extensively the processes involved? One possible
847 reason might be that language is foundational to abstract
848 thought and that the modality is processed early in the
849 cognitive stream and then filtered out as to leave only abstract
850 reasoning at play. Current research brings evidence for both
851 function-specificity in some of the key language brain areas but
852 also language modality-specific effects. Indeed, the left-
853 lateralized language network has repeatedly been shown to be

854 activated regardless of language modality and supporting
855 similar cognitive processes across modalities [16-18, 58-62].
856 This supports the idea that core language processes are
857 subtended similarly and in similar brain regions regardless of
858 modality. However, there is also evidence for language
859 modality-specific activations such as greater bilateral network
860 recruitment with additional spatial-related processes in the
861 parietal lobes for sign language processing. Morford and
862 colleagues [63] have found modality specific interference
863 effects, suggesting that the modality is not completely filtered
864 out early in the decoding process. The other possibility is that,
865 regardless of the language modality and its processing,
866 something in the characteristics of the operation themselves
867 dictate how the core systems are being recruited to support
868 proficiency.

869 Because this is the first ERP study investigating arithmetic
870 in Deaf native signers, we want to acknowledge that much is
871 still to be investigated. Even if we do not evidence differences
872 between groups in our paradigm using visual input and Arabic
873 digits, we want to acknowledge that the question of the impact
874 of language modality is still open. Indeed, more studies
875 investigating more subtly the presentation modality could
876 inform on the role of language modality as well as the
877 abstractness of arithmetic processing. For example, it would be
878 relevant to investigate how presenting arithmetic problems in
879 the language modality of the participants (i.e., in spoken vs.
880 signed language) might modulate the cognitive processes
881 recruited.

882 Our findings are also relevant to the Deaf population and
883 the education of the deaf child. Visual-signed languages are still
884 not fully recognized around the world, and many deaf children
885 are still withheld from full language access based on
886 preconceptions about sign languages. Here, we selected highly
887 proficient ASL signers with profound to severe hearing loss,
888 who reported being exposed to ASL prior to age 2 and having
889 received instruction in ASL through their formative years.
890 However, their behavioral and neural profile appears
891 exceptionally in line with that presented by our hearing group.
892 These results, along with those on ASL language processing,
893 once more dispel the belief that exposure to a sign language
894 should be withheld. On the contrary, these results support the
895 idea that the brain does not care about language modality,
896 provided it is given optimal access to language. We find that the
897 attentional processes and the differentiation in the neural
898 recruitment for arithmetic processing appears to be immune to
899 language modality. We hope that this is only the first of many
900 studies further investigating the role of language modality on
901 the neurocognitive processes supporting arithmetic.

902 5. Conclusions

903 In summary, to answer the question of whether Deaf native
904 signers and English-speakers process arithmetic operations
905 similarly, we find evidence for similar distinctions between

906 operations for the two groups. Further, the pattern of
907 modulations with problem size are also similar across groups.
908 Indeed, in both groups, there was an early operation-dependent
909 frontal modulation and a posterior size-dependent modulation
910 only for subtraction problems, suggesting a similar operation-
911 specific quantity modulation. Our results therefore bring no
912 evidence indicating that the two linguistic groups resort to
913 substantially different strategies and that using a sign language
914 impacts the cognitive processes recruited in solving arithmetic
915 operations.

916
917 **Author Contributions:** Conceptualization, I.B.; methodology, I.B. and L.C.Q.; formal
918 analysis, I.B., M.M., and S.E.K.; investigation, I.B., S.J.S., and S.E.K.; resources, I.B.
919 and L.C.Q.; data curation, I.B.; writing—original draft preparation, I.B.; writing—
920 review and editing, I.B., M.M., L.C.Q., S.E.K., and S.J.S.; visualization, I.B.;
921 supervision, I.B.; project administration, S.J.S. and I.B.; funding acquisition, I.B. and
922 L.C.Q.; All authors have read and agreed to the published version of the manuscript.

923 **Funding:** This research was funded by a Gallaudet University Small Research Grant
924 (SRG) awarded to the first author. Makoto Miyakoshi is supported by NIH
925 5R01NS047293-16 ‘EEGLAB: Software for Analysis of Human Brain Dynamics’ and a
926 generous gift of The Swartz Foundation (Oldfield, New York).

927 **Institutional Review Board Statement:** The study was conducted according to the
928 guidelines of the Declaration of Helsinki and approved by the Institutional Review
929 Board of Gallaudet University (protocol code 3082 and April 18, 2018).

930 **Informed Consent Statement:** Written informed consent was obtained from all
931 subjects involved in the study.

932 **Data Availability Statement:** The data presented in this study are available on
933 request from the corresponding author.

934 **Acknowledgments:** We wish to thank our participants for joining the study as well
935 as the following research assistants who have contributed to the data collection
936 process: Lauren Berger, Hannah Carter, Kayla Scott, and Lucas Lancaster. We would
937 like to thank the members of the Action and Brain Lab at Gallaudet University for
938 providing technical assistance.

939 **Conflicts of Interest:** The authors declare no conflict of interest.

940 Appendix A

941 List of problems and their proposed answers.

Subtraction	Large	14	8	6	5 (z-1)	7 (z+1)
Subtraction	Large	15	9	6	5 (z-1)	7 (z+1)
Subtraction	Large	15	8	7	6 (z-1)	8 (z+1)
Subtraction	Large	16	9	7	6 (z-1)	8 (z+1)
Subtraction	Large	17	9	8	7 (z-1)	9 (z+1)
Subtraction	Large	13	6	7	5 (z-2)	9 (z+2)
Subtraction	Large	14	6	8	6 (z-2)	10 (z+2)
Subtraction	Large	15	6	9	7 (z-2)	11 (z+2)
Subtraction	Large	15	7	8	6 (z-2)	10 (z+2)
Subtraction	Large	16	7	9	7 (z-2)	11 (z+2)
Subtraction	Large	17	8	9	7 (z-2)	11 (z+2)
Subtraction	Extra-Large	42	6	36	34 (z-2)	38 (z+2)
Subtraction	Extra-Large	48	6	42	40 (z-2)	44 (z+2)
Subtraction	Extra-Large	54	6	48	46 (z-2)	50 (z+2)
Subtraction	Extra-Large	56	7	49	47 (z-2)	51 (z+2)
Subtraction	Extra-Large	63	7	56	54 (z-2)	58 (z+2)
Subtraction	Extra-Large	72	8	64	62 (z-2)	66 (z+2)
Subtraction	Extra-Large	42	7	35	33 (z-2)	37 (z+2)
Subtraction	Extra-Large	48	8	40	38 (z-2)	42 (z+2)
Subtraction	Extra-Large	54	9	45	43 (z-2)	47 (z+2)
Subtraction	Extra-Large	56	8	48	46 (z-2)	50 (z+2)
Subtraction	Extra-Large	63	9	54	52 (z-2)	56 (z+2)
Subtraction	Extra-Large	72	9	63	61 (z-2)	65 (z+2)
Multiplication	Small	2	3	6	3 (x-1)	9 (x+1)
Multiplication	Small	2	4	8	4 (x-1)	12 (x+1)
Multiplication	Small	2	5	10	5 (x-1)	15 (x+1)
Multiplication	Small	3	4	12	8 (x-1)	16 (x+1)
Multiplication	Small	3	5	15	10 (x-1)	20 (x+1)
Multiplication	Small	4	5	20	15 (x-1)	25 (x+1)
Multiplication	Small	3	2	6	4 (x-1)	8 (x+1)
Multiplication	Small	4	2	8	6 (x-1)	10 (x+1)
Multiplication	Small	5	2	10	8 (x-1)	12 (x+1)
Multiplication	Small	4	3	12	9 (x-1)	15 (x+1)
Multiplication	Small	5	3	15	12 (x-1)	18 (x+1)
Multiplication	Small	5	4	20	16 (x-1)	24 (x+1)
Multiplication	Large	6	7	42	35 (x-1)	49 (x+1)
Multiplication	Large	6	8	48	40 (x-1)	56 (x+1)
Multiplication	Large	6	9	54	45 (x-1)	63 (x+1)
Multiplication	Large	7	8	56	48 (x-1)	64 (x+1)
Multiplication	Large	7	9	63	54 (x-1)	72 (x+1)
Multiplication	Large	8	9	72	63 (x-1)	81 (x+1)
Multiplication	Large	7	6	42	36 (x-1)	48 (x+1)
Multiplication	Large	8	6	48	42 (x-1)	54 (x+1)
Multiplication	Large	9	6	54	48 (x-1)	60 (x+1)
Multiplication	Large	8	7	56	49 (x-1)	63 (x+1)
Multiplication	Large	9	7	63	56 (x-1)	70 (x+1)
Multiplication	Large	9	8	72	64 (x-1)	80 (x+1)

942

943 References

- De Smedt, B. & Grabner, R. H. Application of Neuroscience to Mathematics Education. in *The Oxford Handbook of Numerical Cognition* (eds. Cohen Kadosh, R. & Dowker, A.) 613-634 (Oxford University Press, 2015).
- Ischebeck, A. *et al.* How specifically do we learn? Imaging the learning of multiplication and subtraction. *Neuroimage* **30**, 1365-75 (2006). <https://doi.org/10.1016/j.neuroimage.2005.11.016>
- Zamarian, L., Ischebeck, A. & Delazer, M. Neuroscience of learning arithmetic--evidence from brain imaging studies. *Neurosci. Biobehav. Rev.* **33**, 909-25 (2009). <https://doi.org/10.1016/j.neubiorev.2009.03.005>
- Ischebeck, A., Zamarian, L., Egger, K., Schocke, M. & Delazer, M. Imaging early practice effects in arithmetic. *Neuroimage* **36**, 993-1003 (2007). <https://doi.org/10.1016/j.neuroimage.2007.03.051>
- Delazer, M. *et al.* Learning by strategies and learning by drill - Evidence from an fMRI study. *Neuroimage* **25**, 838-849 (2005). <https://doi.org/10.1016/j.neuroimage.2004.12.009>
- Tang, Y. *et al.* Arithmetic processing in the brain shaped by cultures. *Proc. Natl. Acad. Sci.* **103**, 10775-80 (2006). <https://doi.org/10.1073/pnas.0604416103>
- Petitto, L.-A. Are signed languages 'real' languages? *Repr. from Signpost (International Q. Sign Linguist. Assoc.* **7**, 1-10 (1994).
- Kolb, B., Harker, A. & Gibb, R. Principles of plasticity in the developing brain. *Dev. Med. Child Neurol.* **59**, 1218-1223 (2017). <https://doi.org/10.1111/dmnc.13546>

960

9. Emmorey, K., Klima, E. & Hickok, G. Mental rotation within linguistic and non-linguistic domains in users of American sign language. *Cognition* **68**, 221–246 (1998). [https://doi.org/10.1016/S0010-0277\(98\)00054-7](https://doi.org/10.1016/S0010-0277(98)00054-7)
10. Emmorey, K., Kosslyn, S. M. & Bellugi, U. Visual imagery and visual-spatial language: Enhanced imagery abilities in deaf and hearing ASL signers. *Cognition* **46**, 139–181 (1993). [https://doi.org/10.1016/0010-0277\(93\)90017-P](https://doi.org/10.1016/0010-0277(93)90017-P)
11. Talbot, K. F. & Haude, R. H. The relation between sign language skill and spatial visualization ability: mental rotation of three-dimensional objects. *Perceptual Mot. Ski.* **77**, 1387–1391 (1993). <https://doi.org/10.2466/pms.1993.77.3f.1387>
12. Wilson, M. & Emmorey, K. A visuospatial ‘phonological loop’ in working memory: evidence from American Sign Language. *Mem. Cognit.* **25**, 313–320 (1997). <https://doi.org/10.3758/BF03211287>
13. Corina, D. P. & Knapp, H. P. Sign language processing and the mirror neuron system. *Cortex* **42**, 529–539 (2006). [https://doi.org/10.1016/S0010-9452\(08\)70393-9](https://doi.org/10.1016/S0010-9452(08)70393-9)
14. Neville, H. J. *et al.* Cerebral organization for language in deaf and hearing subjects: biological constraints and effects of experience. *Proc. Natl. Acad. Sci.* **95**, 922–9 (1998). <https://doi.org/10.1073/pnas.95.3.922>
15. Corina, D. P. Studies of Neural Processing in Deaf Signers: Toward a Neurocognitive Model of Language Processing in the Deaf. *J. Deaf Stud. Deaf Educ.* **3**, 35–48 (1998). <https://www.jstor.org/stable/23805414>
16. Petitto, L.-A. *et al.* Speech-like cerebral activity in profoundly deaf people processing signed languages: implications for the neural basis of human language. *Proc. Natl. Acad. Sci.* **97**, 13961–6 (2000). <https://doi.org/10.1073/pnas.97.25.13961>
17. Petitto, L.-A. *et al.* Visual sign phonology: insights into human reading and language from a natural soundless phonology. *WIREs Cogn. Sci.* (2016). <https://doi.org/10.1002/wcs.1404>
18. Emmorey, K. The Neurobiology of Sign Language. *Brain Mapping: An Encyclopedic Reference* **3**, (Elsevier Inc., 2015).
19. Fehr, T., Code, C. & Herrmann, M. Common brain regions underlying different arithmetic operations as revealed by conjunct fMRI-BOLD activation. *Brain Res.* **1172**, 93–102 (2007). <https://doi.org/10.1016/j.brainres.2007.07.043>
20. Rosenberg-Lee, M., Lovett, M. C. & Anderson, J. R. Neural correlates of arithmetic calculation strategies. *Cogn. Affect. Behav. Neurosci.* **9**, 270–285 (2009). <https://doi.org/10.3758/CABN.9.3.270>
21. Arsalidou, M. & Taylor, M. J. Is $2+2=4$? Meta-analyses of brain areas needed for numbers and calculations. *Neuroimage* **54**, 2382–93 (2011). <https://doi.org/10.1016/j.neuroimage.2010.10.009>
22. Yu, X. *et al.* Dissociation of subtraction and multiplication in the right parietal cortex: evidence from intraoperative cortical electrostimulation. *Neuropsychologia* **49**, 2889–95 (2011). <https://doi.org/10.1016/j.neuropsychologia.2011.06.015>
23. Zhou, X. *et al.* Event-related potentials of single-digit addition, subtraction, and multiplication. *Neuropsychologia* **44**, 2500–7 (2006). <https://doi.org/10.1016/j.neuropsychologia.2006.04.003>
24. Zhou, X. *et al.* Dissociated brain organization for single-digit addition and multiplication. *Neuroimage* **35**, 871–80 (2007). <https://doi.org/10.1016/j.neuroimage.2006.12.017>
25. Jasinski, E. C. & Coch, D. ERPs across arithmetic operations in a delayed answer verification task. *Psychophysiology* **49**, 943–958 (2012). <https://doi.org/10.1111/j.1469-8986.2012.01378.x>
26. Prado, J. *et al.* Distinct representations of subtraction and multiplication in the neural system for numerosity and language. *Hum. Brain Mapp.* **32**, 1932–1947 (2011). <https://doi.org/10.1002/hbm.21159>
27. Seitz, K. & Schumann-Hengsteler, R. Mental multiplication and working memory. *Eur. J. Cogn. Psychol.* **12**, 552–570 (2000). <https://doi.org/10.1080/095414400750050231>
28. Prado, J., Mutreja, R. & Booth, J. R. Developmental dissociation in the neural responses to simple multiplication and subtraction problems. *Dev. Sci.* **17**, 537–552 (2014). <https://doi.org/10.1111/desc.12140>
29. Rivera, S. M., Reiss, A. L., Eckert, M. a & Menon, V. Developmental changes in mental arithmetic: evidence for increased functional specialization in the left inferior parietal cortex. *Cereb. Cortex* **15**, 1779–90 (2005). <https://doi.org/10.1093/cercor/bhi055>
30. Núñez-Peña, M. I., Gracia-Bafalluy, M. & Tubau, E. Individual differences in arithmetic skill reflected in event-related brain potentials. *Int. J. Psychophysiol.* **80**, 143–9 (2011). <https://doi.org/10.1016/j.ijpsycho.2011.02.017>
31. Rosenberg-Lee, M., Barth, M. & Menon, V. What difference does a year of schooling make? Maturation of brain response and connectivity between 2nd and 3rd grades during arithmetic problem solving. *Neuroimage* **57**, 796–808 (2011). <https://doi.org/10.1016/j.ijpsycho.2011.02.017>
32. Núñez-Peña, M. I., Cortinas, M. & Escera, C. Problem size effect and processing strategies in mental arithmetic. *Neuroreport* **17**, 357–360 (2006). <https://doi.org/10.1097/01.wnr.0000203622.24953.c2>
33. Ku, Y., Hong, B., Gao, X. & Gao, S. Spectra-temporal patterns underlying mental addition: An ERP and ERD/ERS study. *Neurosci. Lett.* **472**, 5–10 (2010). <https://doi.org/10.1016/j.neulet.2010.01.040>
34. Dehaene, S. The Organization of Brain Activations in Number Comparison: Event-Related Potentials and the Additive-Factors Method. *J. Cogn. Neurosci.* **8**, 47–68 (1996). <https://doi.org/10.1162/jocn.1996.8.1.47>
35. Hinault, T. & Lemaire, P. What does EEG tell us about arithmetic strategies? A review. *Int. J. Psychophysiol.* (2016). <https://doi.org/10.1016/j.ijpsycho.2016.05.006>
36. Muluh, E. T., Vaughan, C. L. & John, L. R. High resolution event-related potentials analysis of the arithmetic-operation effect in mental arithmetic. *Clin. Neurophysiol.* **122**, 518–529 (2011). <https://doi.org/10.1016/j.clinph.2010.08.008>
37. Kiefer, M. & Dehaene, S. The Time Course of Parietal Activation in Single-digit Multiplication: Evidence from Event-related Potentials. *Mathematical Cognition* **3**, 1–30 (1997). <https://doi.org/10.1080/135467997387461>
38. Campbell, J. I. D. & Oliphant, M. Representation and retrieval of arithmetic facts: a network-interference model and simulation. In *The Nature and Origins of Mathematical Cognition* (ed. Campbell, J. I. D.) 331–364 (Elsevier Science Publisher B.V., 1992). [https://doi.org/10.1016/S0166-4115\(08\)60891-2](https://doi.org/10.1016/S0166-4115(08)60891-2)

- 1031 39. Taillan, J., Ardiale, E. & Lemaire, P. Relationships between strategy switching and strategy switch costs in
1032 young and older adults: A study in arithmetic problem solving. *Exp. Aging Res.* **41**, 136–156 (2015).
1033 <https://doi.org/10.1080/0361073X.2015.1001651>
- 1034 40. Benjamini, Y., & Hochberg, Y. (1995). Controlling the false discovery rate: a practical and powerful approach
1035 to multiple testing. *Journal of the Royal Statistical Society: series B (Methodological)* 57(1), 289–300. <https://doi.org/10.1111/j.2517-6161.1995.tb02031.x>
- 1036 41. Fayol, M. & Thevenot, C. The use of procedural knowledge in simple addition and subtraction
1037 problems. *Cognition* **123**, 392–403 (2012). <https://doi.org/10.1016/j.cognition.2012.02.008>
- 1038 42. Andin, J., Elwér, Å. & Mäki-Torkko, E. Arithmetic in the adult deaf signing brain. *J. Neurosci. Res.* **98**, 643–
1039 654 (2020). <https://publons.com/publon/10.1002/jnr.24569>
- 1040 43. Amano, K. *et al.* Estimation of the timing of human visual perception from magnetoencephalography. *J.*
1041 *Neurosci.* **26**, 3981–3991 (2006). <https://doi.org/10.1523/JNEUROSCI.4343-05.2006>
- 1042 44. Taillan, J., Dufau, S. & Lemaire, P. How Do We Choose Among Strategies to Accomplish Cognitive Tasks?
1043 Evidence From Behavioral and Event-Related Potential Data in Arithmetic Problem Solving. *Mind, Brain,*
1044 *Educ.* **9**, 222–231 (2015). <https://doi.org/10.1111/mbe.12095>
- 1045 45. El Yagoubi, R., Lemaire, P. & Besson, M. Different brain mechanisms mediate two strategies in arithmetic:
1046 Evidence from event-related brain potentials. *Neuropsychologia* **41**, 855–862 (2003). [https://doi.org/10.1016/S0028-3932\(02\)00180-X](https://doi.org/10.1016/S0028-3932(02)00180-X)
- 1047 46. Luo, W., Liu, D., He, W., Tao, W. & Luo, Y. Dissociated brain potentials for two calculation strategies.
1048 *Neuroreport* **20**, 360–364 (2009). <https://doi.org/10.1097/WNR.0b013e328323d737>
- 1049 47. Stanesco-Cosson, R. *et al.* Understanding dissociations in dyscalculia: a brain imaging study of the impact of
1050 number size on the cerebral networks for exact and approximate calculation. *Brain* **123**, 2240–55 (2000).
1051 <https://doi.org/10.1093/brain/123.11.2240>
- 1052 48. He, W. Q., Luo, W. B., He, H. M., Chen, X. & Zhang, D. J. N170 effects during exact and approximate
1053 calculation tasks: An ERP study. *Neuroreport* **22**, 437–441 (2011). doi: 10.1097/WNR.0b013e32834702c1
- 1054 49. Núñez-Peña, M. I., Honrubia-Serrano, M. L. & Escera, C. Problem size effect in additions and subtractions:
1055 An event-related potential study. *Neurosci. Lett.* **373**, 21–25 (2005).
1056 <https://doi.org/10.1016/j.neulet.2004.09.053>
- 1057 50. Neville, H. J., Schmidt, A. & Kutas, M. Altered visual-evoked potentials in congenitally deaf adults. *Brain Res.*
1058 **266**, 127–132 (1983). [https://doi.org/10.1016/0006-8993\(83\)91314-8](https://doi.org/10.1016/0006-8993(83)91314-8)
- 1059 51. Yukhymenko, L. I. Cortical Visual Evoked Potentials in Subjects with Auditory Deprivation (Congenital
1060 Deafness). *Neurophysiology* **49**, 240–243 (2017). <https://doi.org/10.1007/s11062-017-9676-0>
- 1061 52. Uittenhove, K., Poletti, C., Dufau, S. & Lemaire, P. The time course of strategy sequential difficulty effects :
1062 An ERP study in arithmetic. *Exp. brain Res.* **227**, 1–8 (2013). <https://doi.org/10.1007/s00221-012-3397-9>
- 1063 53. Hinault, T., Dufau, S. & Lemaire, P. Sequential modulations of poorer-strategy effects during strategy
1064 execution: An event-related potential study in arithmetic. *Brain Cogn.* **91**, 123–130 (2014).
1065 <https://doi.org/10.1016/j.bandc.2014.09.001>
- 1066 54. Polich, J. Updating P300: an integrative theory of P3a and P3b. *Clin. Neurophysiol.* **118**, 2128–48 (2007).
1067 <https://doi.org/10.1016/j.clinph.2007.04.019>
- 1068 55. Quandt, L. C. & Kubicek, E. Sensorimotor characteristics of sign translations modulate EEG when deaf
1069 signers read English. *Brain Lang.* **187**, 9–17 (2018). <https://doi.org/10.1016/j.bandl.2018.10.001>
- 1070 56. Friedman, D. & Johnson, R. Event-related potential (ERP) studies of memory encoding and retrieval: A
1071 selective review. *Microsc. Res. Tech.* **51**, 6–28 (2000). [https://doi.org/10.1002/1097-0029\(20001001\)51:1<6::AID-JEMT2>3.0.CO;2-R](https://doi.org/10.1002/1097-0029(20001001)51:1<6::AID-JEMT2>3.0.CO;2-R)
- 1072 57. Dehaene, S. Evolution of Human Cortical Circuits for Reading and Arithmetic: The ‘neuronal recycling’
1073 hypothesis. in *From Monkey Brain to Human Brain* 133–157 (2005). doi:10.7551/mitpress/3136.003.0012
- 1074 58. Petitto, L.-A. *et al.* Bilingual signed and spoken language acquisition from birth: Implications for the
1075 mechanisms underlying early bilingual language acquisition. *J. Child Lang.* **28**, 453–496 (2001). doi:10.1017/S0305000901004718
- 1076 59. Clark, M. D. *et al.* The Importance of Early Sign Language Acquisition for Deaf Readers. *Read. Writ. Q.* **32**,
1077 127–151 (2016). <https://doi.org/10.1080/10573569.2013.878123>
- 1078 60. Holmer, E., Heimann, M. & Rudner, M. Evidence of an association between sign language phonological
1079 awareness and word reading in deaf and hard-of-hearing children. *Res. Dev. Disabil.* **48**, 145–159 (2016).
1080 <https://doi.org/10.1016/j.ridd.2015.10.008>
- 1081 61. Mayberry, R. I. When timing is everything: Age of first-language acquisition effects on second-language
1082 learning. *Appl. Psycholinguist.* **28**, 537–549 (2007). doi:10.1017/S0142716407070294
- 1083 62. Padden, C. & Ramsey, C. American Sign Language and Reading Ability in Deaf Children. in *Language*
1084 *acquisition by eye* (ed. Mayberry, R. I.) 165–189 (Lawrence Erlbaum Associates, 2000).
- 1085 63. Morford, J. P., Wilkinson, E., Villwock, A., Piñar, P. & Kroll, J. F. When deaf signers read English: Do written
1086 words activate their sign translations? *Cognition* **118**, 286–292 (2011).
1087 <https://doi.org/10.1016/j.cognition.2010.11.006>
- 1088
1089
1090
1091
1092
1093